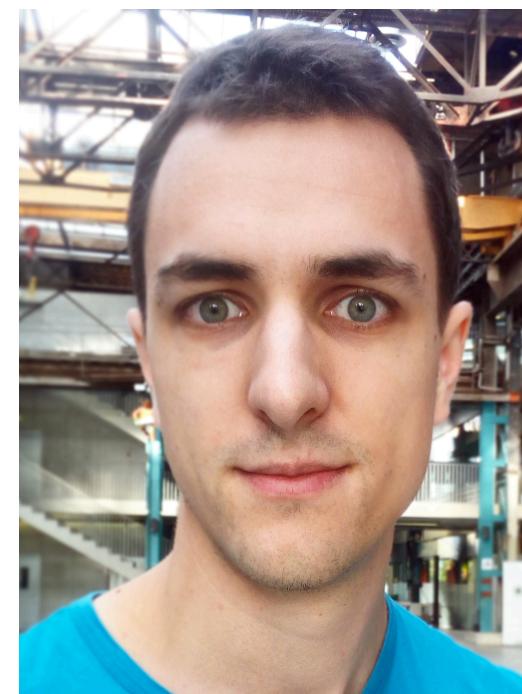


# On the Unusual Effectiveness of Type-aware Operator Mutations for Testing SMT Solvers

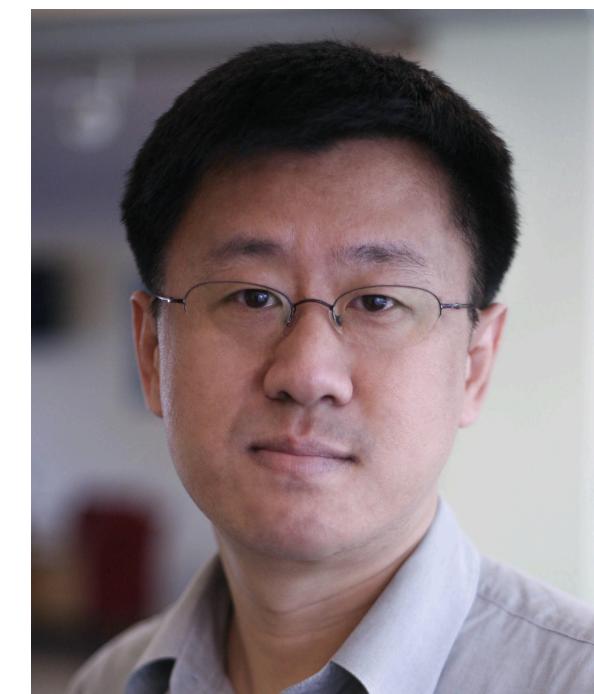
Dominik Winterer\*  
ETH Zurich, Switzerland



Chengyu Zhang\*  
East China Normal University, China  
(\*Equal contributions)



Zhendong Su  
ETH Zurich, Switzerland



# SMT Problem

$$\varphi : x > 0 \wedge x < 0$$

# SMT Problem

$$\varphi : x > 0 \wedge x < 0$$

**UNSAT**

# SMT Problem

$$\varphi : x > 0 \wedge x < 1$$

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**SAT**

# SMT Problem

$$x = 0.5$$

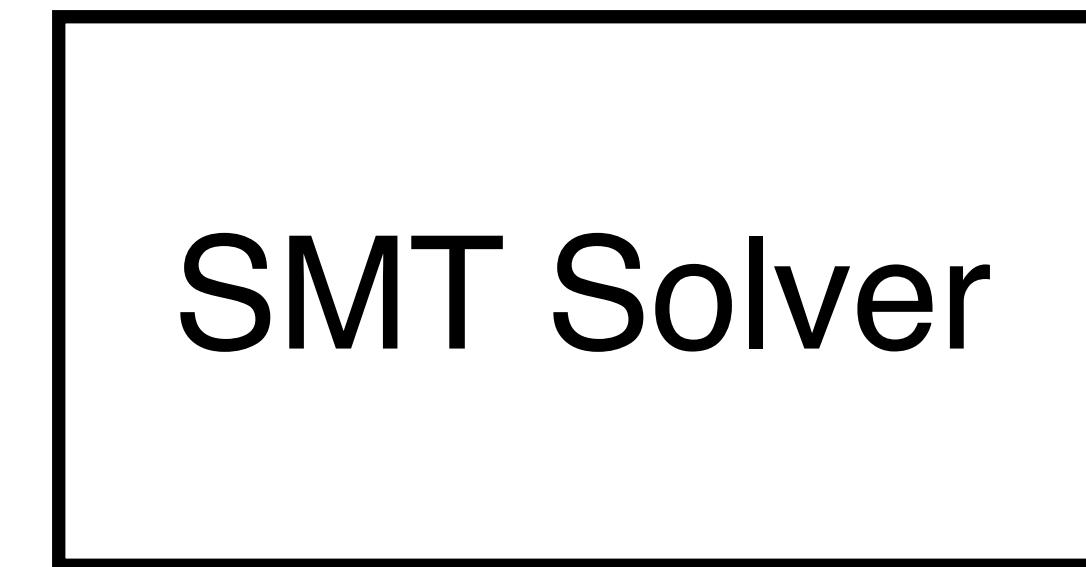
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**SAT**

# SMT Solver

SMT Solver

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$$\varphi : x > 0 \wedge x < 1 \rightarrow$$


# SMT Solver

$$\varphi : x > 0 \wedge x < 1 \rightarrow \boxed{\text{SMT Solver}} \rightarrow \text{SAT}$$

# SMT Solver

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Symbolic  
Execution

SMT Solver

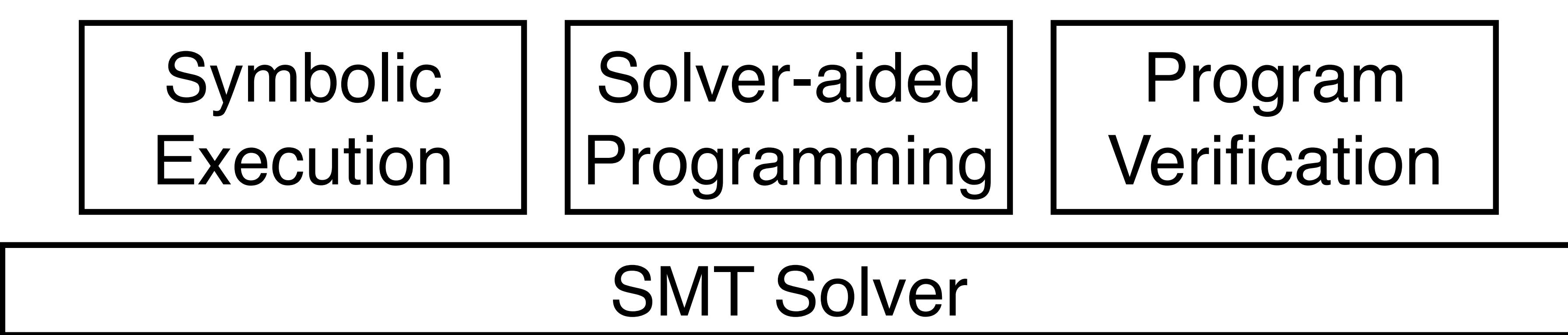
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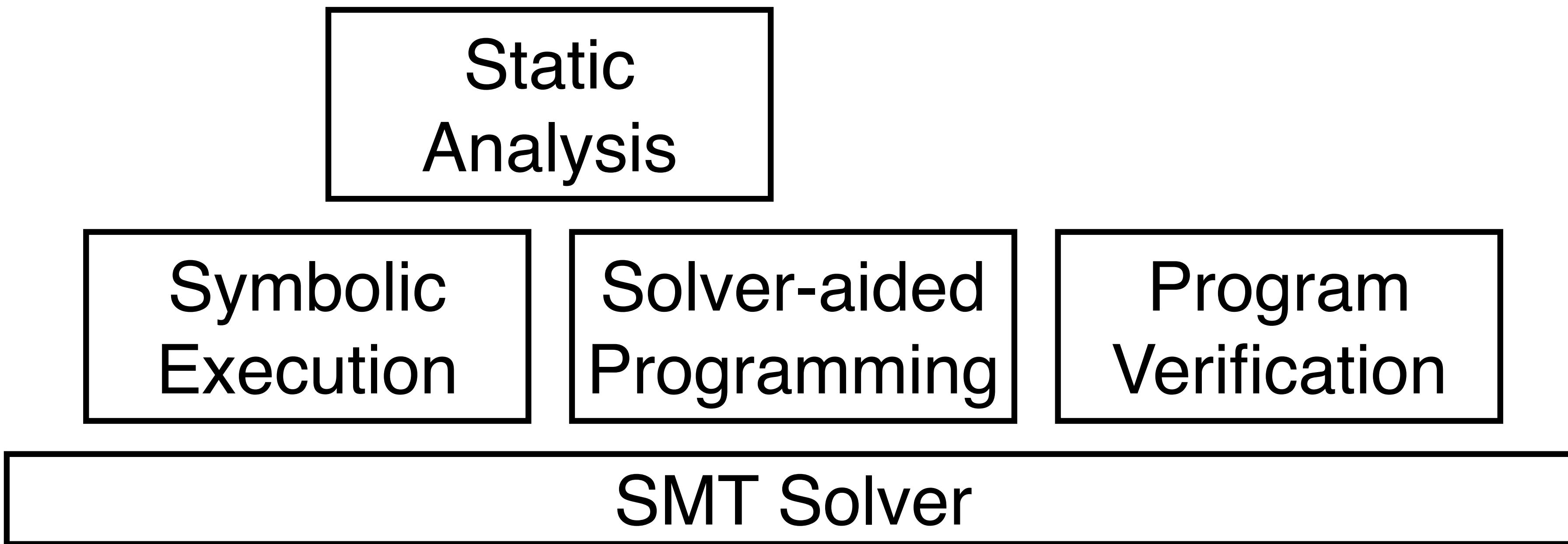
Solver-aided  
Programming

SMT Solver

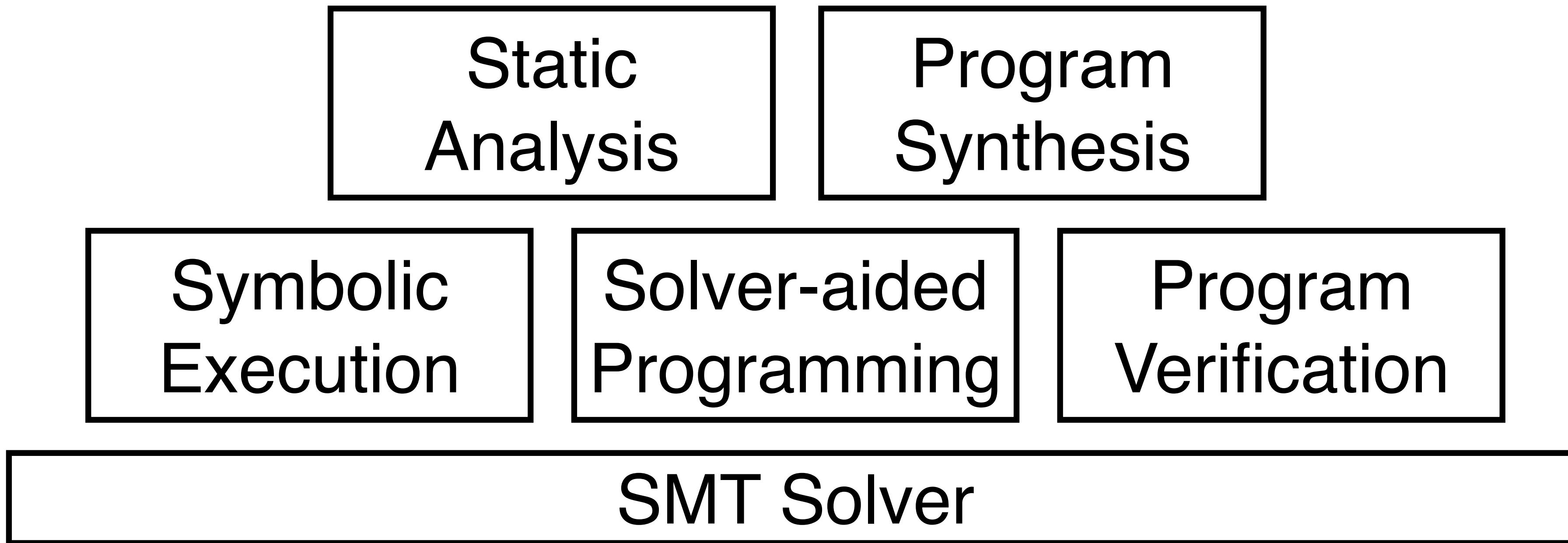
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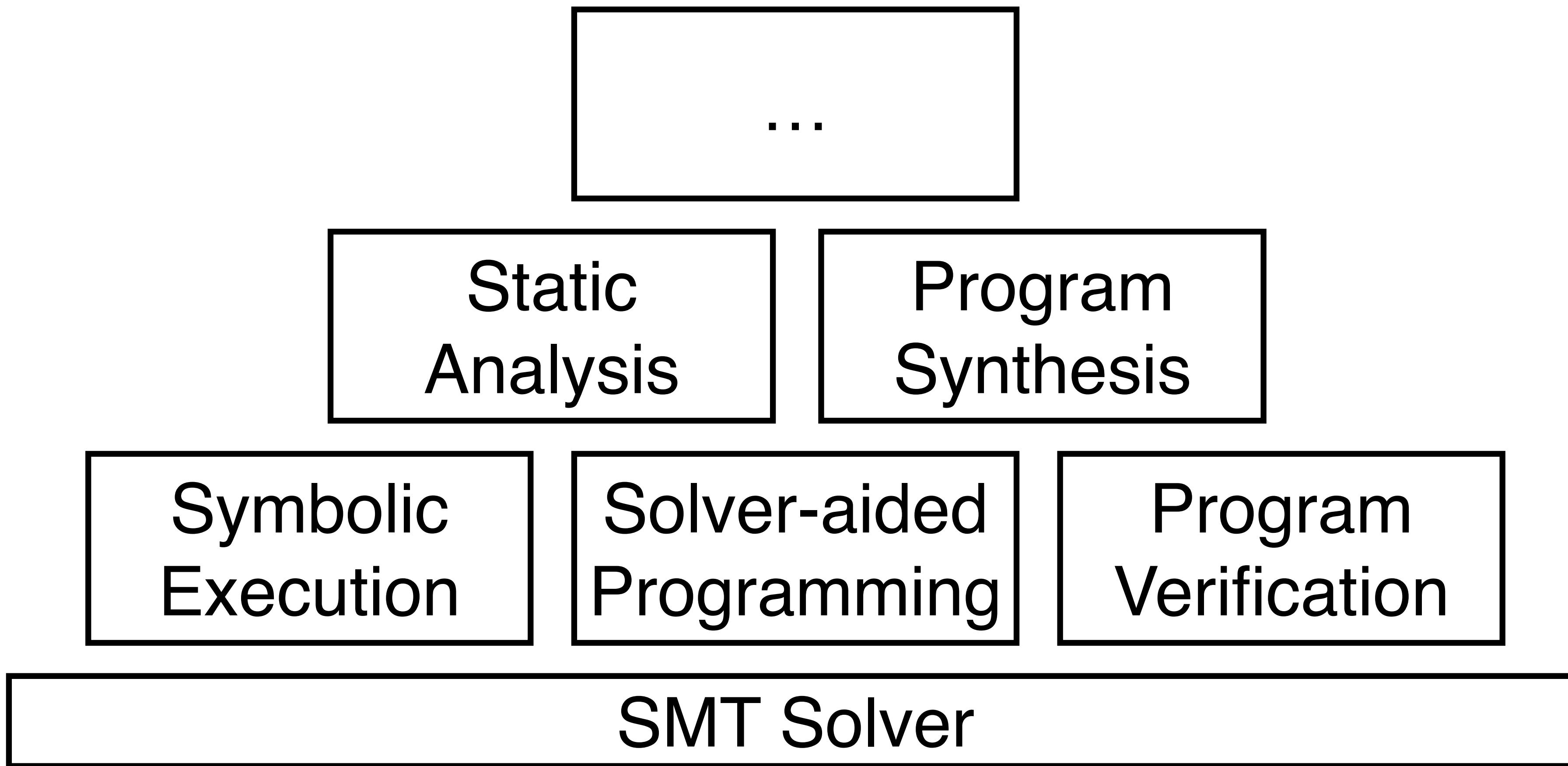
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# SMT-LIB language

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# SMT Solver Bug

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```
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unsat ✓
```

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<https://github.com/Z3Prover/z3/issues/3973>

# Related Work

Approach	Confirmed Bugs in Z3		Confirmed Bugs in CVC4	
	soundness	all	soundness	all
StringFuzz [1]	0	0	-	-
BanditFuzz [2]	0	0	-	-
Bugariu et al. [3]	1	3	0	0
YinYang [4]	24	36	5	8
STORM [5]	17	21	0	0

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## SIMPLE BUT UNUSUAL EFFECTIVE APPROACH

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                            <  
                          >=   
                          <=

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<https://github.com/Z3Prover/z3/issues/3973>

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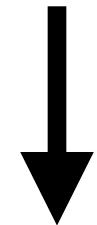
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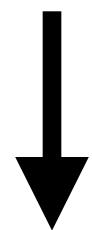
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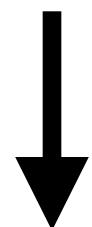
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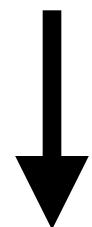
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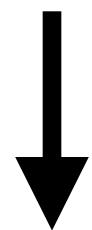
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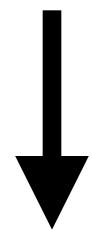
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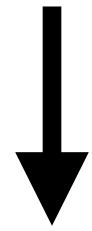
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<https://github.com/Z3Prover/z3/issues/2715>

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- Bug hunting: Sep 2019 - Oct 2020
- Testing targets: Z3 and CVC4
- Seeds: SMT-LIB benchmarks (300k+ formulas)

# Bug Findings

Status	Z3	CVC4	Total
Reported	811	281	1,092
Confirmed	578	241	819
Fixed	521	164	685
Duplicate	85	18	106

Bug status as of 30 Oct 2020

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# Bug Findings

<b>#Options</b>	<b>Z3</b>	<b>CVC4</b>	<b>Total</b>
Default	388	101	489
1	109	67	176
2	45	31	76
$\geq 3$	36	42	78

Number of options for triggering the bugs

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Confirmed bugs in the default modes of the solvers

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OpFuzz found many more soundness bugs in Z3 and CVC4's default modes than all previous approaches

# Z3 Soundness Bug #2832

```
$ cat bug.smt2
(declare-const a (_ BitVec 8))
(declare-const b (_ BitVec 8))
(declare-const c (_ BitVec 8))
(assert (= (bvxnor a b c)
            (bvxnor (bvxnor a b) c)))
(check-sat)
```

```
$ cvc4 bug.smt2
sat ✓
```

```
$ z3 bug.smt2
unsat ✗
```

<https://github.com/Z3Prover/z3/issues/2832>

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# Z3 Soundness Bug #2832

```
(bvxnor a b c) ≠ (not (bvxor a b c))
```

# Z3 Soundness Bug #2832

```
(bvxnor a b c) ≠ (not (bvxor a b c))
```

```
(bvxnor true true true) = (not (bvxor true true true))
```

# Z3 Soundness Bug #2832

```
(bvxnor a b c) ≠ (not (bvxor a b c))
```

```
(bvxnor true true true) = (not (bvxor true true true))  
(bvnxor (bvnxor true true) true)) = (not (bvxor (bvxor true true) true))
```

# Z3 Soundness Bug #2832

```
(bvxnor a b c) ≠ (not (bvxor a b c))
```

```
(bvxnor true true true) = (not (bvxor true true true))
(bvnxor (bvnxor true true) true)) = (not (bvxor (bvxor true true) true))
(bvnxor true true) = (not (bvxor false true))
```

# Z3 Soundness Bug #2832

```
(bvxnor a b c) ≠ (not (bvxor a b c))
```

```
(bvxnor true true true) = (not (bvxor true true true))
(bvnxor (bvnxor true true) true)) = (not (bvxor (bvxor true true) true))
  (bvnxor true true) = (not (bvxor false true))
                true ≠ false
```

# Z3 Soundness Bug #2832

```
$ cat bug.smt2
(declare-const a (_ BitVec 8))
(declare-const b (_ BitVec 8))
(declare-const c (_ BitVec 8))
(assert (= (bvxnor a b c)
            (bvxnor (bvxnor a b) c)))
(check-sat)
```

```
$ cvc4 bug.smt2
sat ✓
```

```
$ z3 bug.smt2
unsat ✗
```

Root Cause: **Unsound rewriter**

<https://github.com/Z3Prover/z3/issues/2832>

# Z3 Soundness Bug #2830

```
$ cat bug.smt2
(declare-fun a () Int)
(declare-fun b (Int) Bool)
(assert (b 0))
(push)
(assert (distinct true (= a 0) (not (b 0))))
(check-sat)
```

```
$ cvc4 bug.smt2
unsat ✓
```

```
$ z3 bug.smt2
sat ✗
```

<https://github.com/Z3Prover/z3/issues/2830>

# Z3 Soundness Bug #2830

```
$ cat bug.smt2
(declare-fun a () Int)
(declare-fun b (Int) Bool)
(assert (b 0))
(push)
(assert (distinct true (= a 0) (not (b 0))))
(check-sat)
```

```
$ cvc4 bug.smt2
unsat ✓
```

```
$ z3 bug.smt2
sat ✗
```

Root Cause: Last argument  
omitted in distinct operator

<https://github.com/Z3Prover/z3/issues/2830>

# CVC4 Soundness Bug #3497

```
$ cat bug.smt2
(declare-fun x () String)
(declare-fun y () String)
(assert (= (str.indexof x y 1)
           (str.len x)))
(assert (str.contains x y))
(check-sat)
```

```
$ z3 bug.smt2
sat ✓
```

```
$ cvc4 bug.smt2
unsat ✗
```

<https://github.com/CVC4/CVC4/issues/3497>

# CVC4 Soundness Bug #3497

```
$ cat bug.smt2
(declare-fun x () String)
(declare-fun y () String)
(assert (= (str.indexof x y 1)
           (str.len x)))
(assert (str.contains x y))
(check-sat)
```

```
$ z3 bug.smt2
sat ✓
```

```
$ cvc4 bug.smt2
unsat ✗
```

<https://github.com/CVC4/CVC4/issues/3497>

# CVC4 Soundness Bug #3497

```
$ cat bug.smt2
(declare-fun x () String)
(declare-fun y () String)
(assert (= (str.indexof x y 1)           (str.indexof x y 1) <= (str.len x)
         (str.len x)))
(assert (str.contains x y))
(check-sat)

$ z3 bug.smt2
sat   ✓

$ cvc4 bug.smt2
unsat ✗
```

<https://github.com/CVC4/CVC4/issues/3497>

# CVC4 Soundness Bug #3497

```
$ cat bug.smt2
(declare-fun x () String)
(declare-fun y () String)
(assert (= (str.indexof x y 1)
           (str.len x)))
(assert (str.contains x y))
(check-sat)
```

(**str.indexof** x y 1) < (**str.len** x)



```
$ z3 bug.smt2
sat ✓
```

**Root Cause: Missed boundary condition**

```
$ cvc4 bug.smt2
unsat ✗
```

<https://github.com/CVC4/CVC4/issues/3497>

# CVC4 Soundness Bug #3497

```
$ cat bug.smt2
(declare-fun x () String)
(declare-fun y () String)
(assert (= (str.indexof x y 1)
           (str.len x)))
(assert (str.contains x y))
(check-sat)
```

```
$ z3 bug.smt2
```

sat



ajreynol commented on Nov 26, 2019

Member

...

Thanks a lot for the bug report, this is fixed in [#3499](#).

```
$ cvc4 bug.smt2
```

unsat



<https://github.com/CVC4/CVC4/issues/3497>

# CVC4 Soundness Bug #4469

```
$ cat bug.smt2
(set-logic QF_AUFBLIA)
(declare-fun a () Int)
(declare-fun b (Int) Int)
(assert (distinct (b a)
                  (b (b a))))))
(check-sat)
```

```
$ z3 bug.smt2
sat ✓
```

```
$ cvc4 bug.smt2
unsat ✗
```

<https://github.com/CVC4/CVC4/issues/4469>

# CVC4 Soundness Bug #4469

```
$ cat bug.smt2
(set-logic QF_AUFBLIA)
(declare-fun a () Int)
(declare-fun b (Int) Int)
(assert (distinct (b a)
                  (b (b a))))))
(check-sat)
```

Labels

bug

major

```
$ z3 bug.smt2
sat ✓
```

```
$ cvc4 bug.smt2
unsat ✗
```

<https://github.com/CVC4/CVC4/issues/4469>

# CVC4 Soundness Bug #3475

```
$ cat bug.smt2
(set-logic ALL)
(declare-fun x () Real)
(assert (< x 0))
(assert (not (= (/ (sqrt x) (sqrt x)) x)))
(check-sat)
```

```
$ z3 bug.smt2
sat ✓
```

```
$ cvc4 bug.smt2
unsat ✗
```

<https://github.com/CVC4/CVC4/issues/3475>

# CVC4 Soundness Bug #3475

```
$ cat bug.smt2
(set-logic ALL)
(declare-fun x () Real)
(assert (< x 0))
(assert (not (= (/ (sqrt x) (sqrt x)) x)))
(check-sat)
```

Formula is satisfiable  
negative x = -1  
 $(/ \sqrt{-1} \sqrt{-1}) = 1$

```
$ z3 bug.smt2
sat ✓
```

```
$ cvc4 bug.smt2
unsat ✗
```

<https://github.com/CVC4/CVC4/issues/3475>

# CVC4 Soundness Bug #3475

Simplification:  
`(sqrt x) = choice real y s.t. x*x = y`

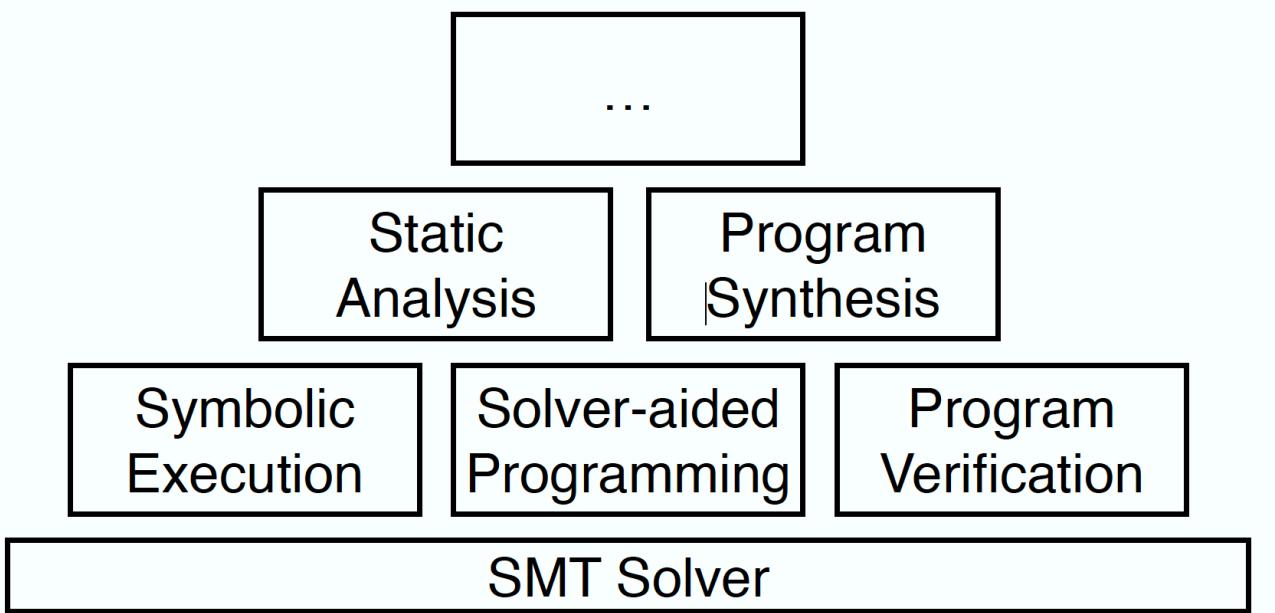
# CVC4 Soundness Bug #3475

```
Simplification:  
(sqrt x) = choice real y s.t. x*x = y
```

Problem: Inadmissible for negative y (since no real x exists)

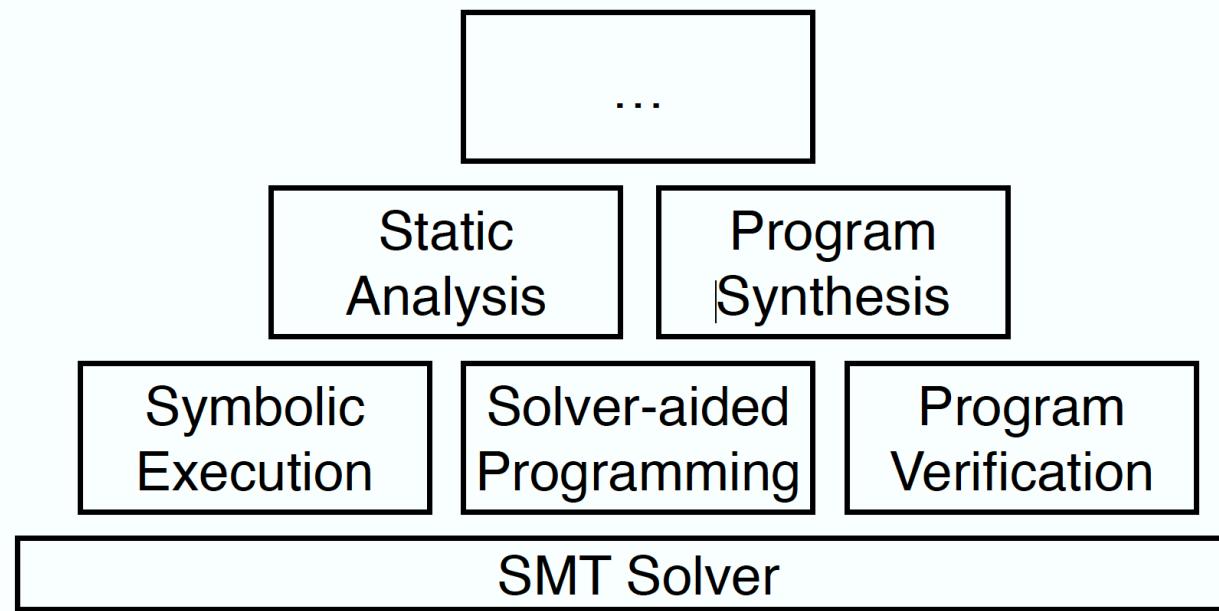
# Summary

## SMT Solver



# Summary

## SMT Solver



## Type-aware operator mutation

```
$ cat > formula.smt2
(assert (forall ((a Int))
  (exist ((b Int))
    (distinct (* 2 b) a))))
(check-sat)
```

→

```
$ cvc4 formula.smt2
sat
```

```
$ z3 formula.smt2
sat ✓
```

```
$ cat > bug.smt2
(assert (forall ((a Int))
  (exist ((b Int))
    (= (* 2 b) a))))
(check-sat)
```

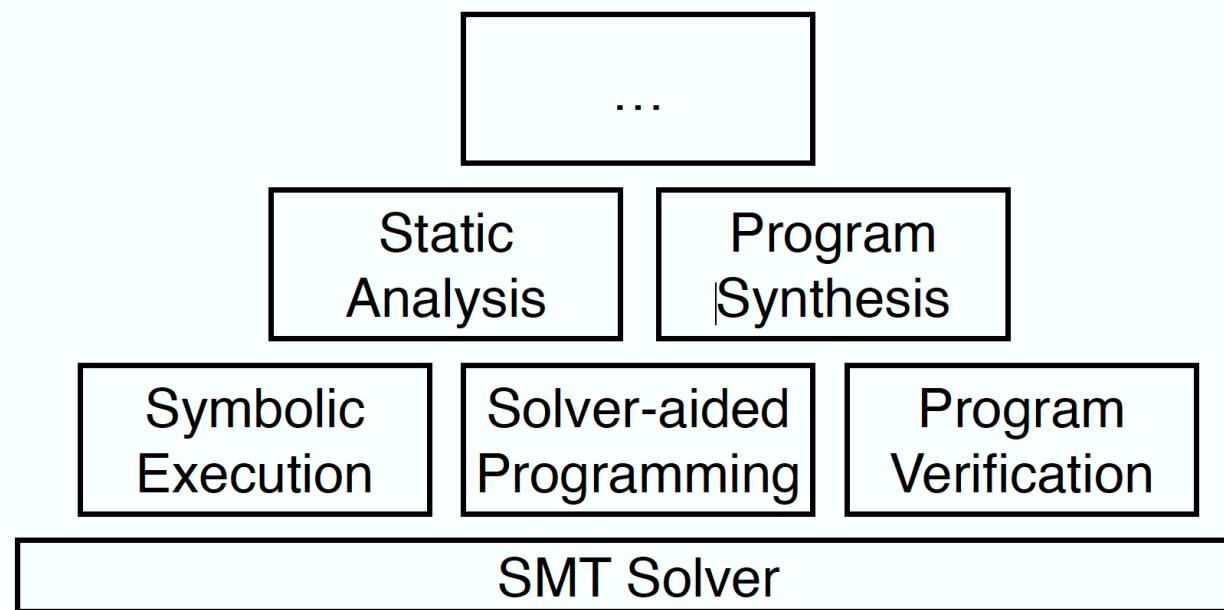
```
$ cvc4 bug.smt2
unsat ✗
```

```
$ z3 bug.smt2
sat ✗
```

<https://github.com/Z3Prover/z3/issues/3973>

# Summary

## SMT Solver



## Type-aware operator mutation

```
$ cat > formula.smt2
(assert (forall ((a Int))
  (exist ((b Int))
    (distinct (* 2 b) a))))
(check-sat)
$ cvc4 formula.smt2
sat
$ z3 formula.smt2
sat
```

→

```
$ cat > bug.smt2
(assert (forall ((a Int))
  (exist ((b Int))
    (= (* 2 b) a))))
(check-sat)
$ cvc4 bug.smt2
unsat ✓
$ z3 bug.smt2
sat ✗
```

<https://github.com/Z3Prover/z3/issues/3973>

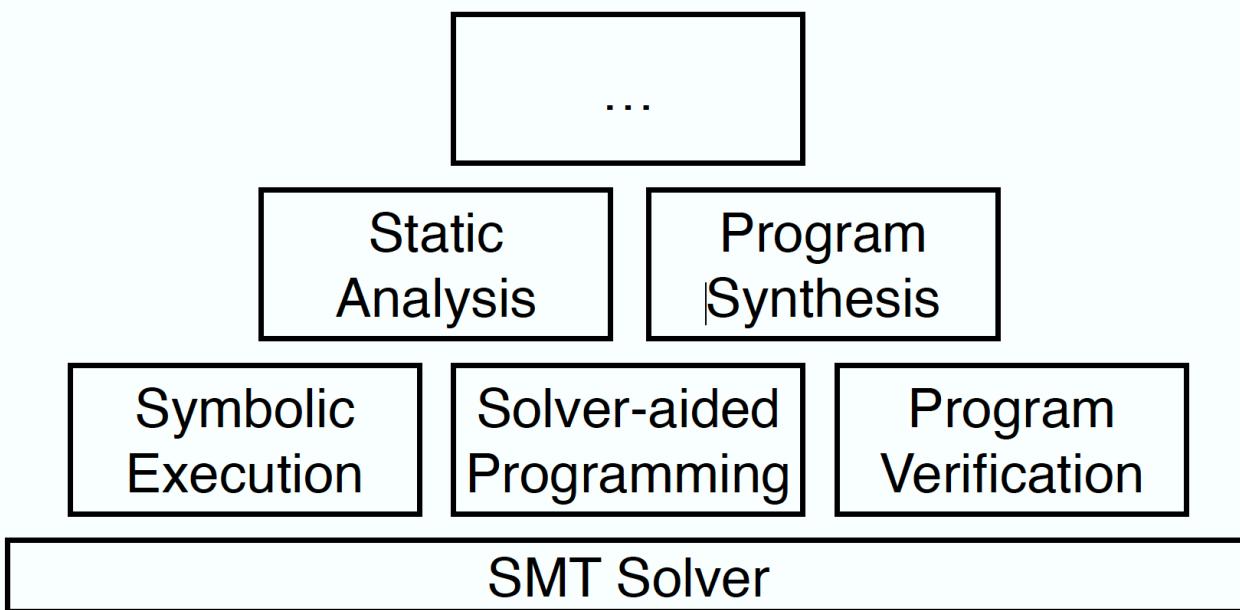
## Bug Findings

Status	Z3	CVC4	Total
Reported	811	281	1,092
Confirmed	578	241	819
Fixed	521	164	106
Duplicate	85	18	79

Bug status as of 30 Oct 2020

# Summary

## SMT Solver



## Type-aware operator mutation

\$ cat > formula.smt2  
 (assert (forall ((a Int))  
 (exist ((b Int))  
 (distinct (\* 2 b) a))))  
 (check-sat)

\$ cvc4 formula.smt2  
 sat

\$ z3 formula.smt2  
 sat

\$ cat > bug.smt2  
 (assert (forall ((a Int))  
 (exist ((b Int))  
 (= (\* 2 b) a))))  
 (check-sat)

\$ cvc4 bug.smt2  
 unsat ✓

\$ z3 bug.smt2  
 sat ✗

<https://github.com/Z3Prover/z3/issues/3973>

## Bug Findings

Status	Z3	CVC4	Total
Reported	811	281	1,092
Confirmed	578	241	819
Fixed	521	164	106
Duplicate	85	18	79

Bug status as of 30 Oct 2020

### Z3 Soundness Bug #2832

\$ cat bug.smt2  
 (declare-const a (\_ BitVec 8))  
 (declare-const b (\_ BitVec 8))  
 (declare-const c (\_ BitVec 8))  
 (assert (= [bxnor a b c])  
 (bxnor (bxnor a b) c)))  
 (check-sat)

\$ cvc4 bug.smt2  
 sat ✓

\$ z3 bug.smt2  
 unsat ✗

<https://github.com/Z3Prover/z3/issues/2832>

### CVC4 Soundness Bug #3497

\$ cat bug.smt2  
 (declare-fun x () String) (str.indexof x y 1) < (str.len x)  
 (declare-fun y () String)  
 (assert (= (str.indexof x y 1) (str.len x)))  
 (assert (str.contains x y))  
 (check-sat)

\$ z3 bug.smt2  
 sat ✓

\$ cvc4 bug.smt2  
 unsat ✗

<https://github.com/CVC4/CVC4/issues/3497>

Root Cause: Missed boundary condition

### CVC4 Soundness Bug #4469

\$ cat bug.smt2  
 (set-logic QF\_AUFBLIA)  
 (declare-fun a () Int)  
 (declare-fun b (Int) Bool)  
 (assert (b 0))  
 (push)  
 (assert (distinct true (= a 0) (not (b 0))))  
 (check-sat)

\$ cvc4 bug.smt2  
 unsat ✓

\$ z3 bug.smt2  
 sat ✗

\$ cvc4 bug.smt2  
 unsat ✗

<https://github.com/CVC4/CVC4/issues/4469>

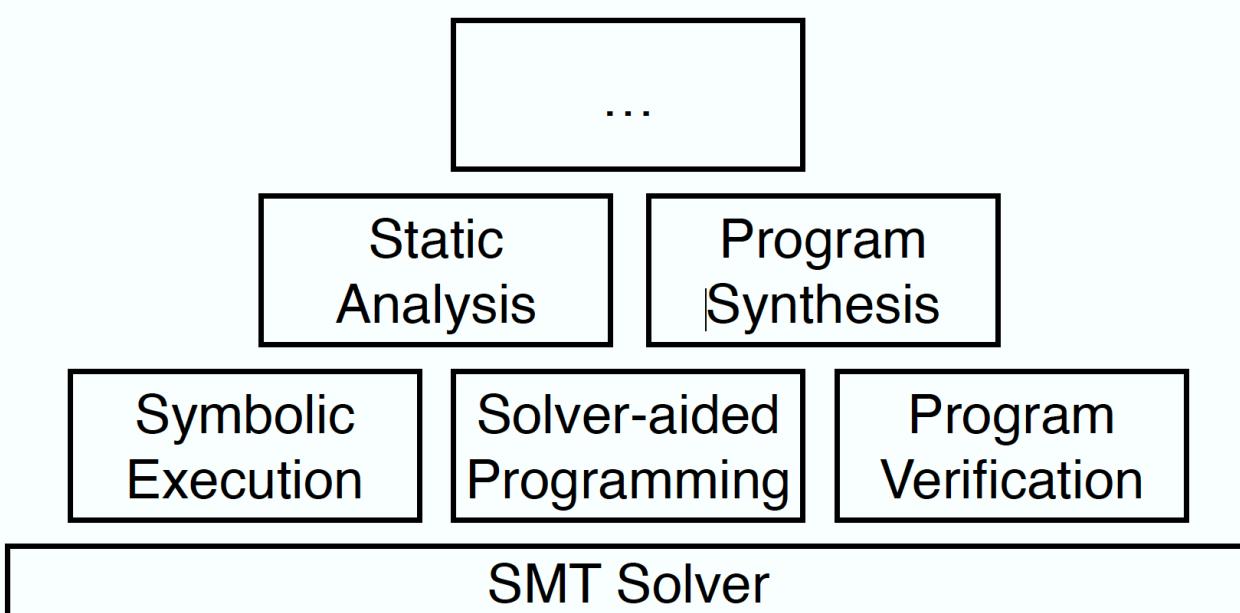
Labels: bug major

Root Cause: Last argument omitted in distinct operator

# Summary



# SMT Solver



# Type-aware operator mutation

```
$ cvc4 formula.smt2  
sat  
  
$ z3 formula.smt2  
sat
```

```
$ cat > bug.smt2
(assert (forall ((a Int))
  (exist ((b Int))
    (= (* 2 b) a))))
(check-sat)
```

```
$ cvc4 bug.smt2  
unsat ✓  
  
$ z3 bug.smt2  
sat ✗
```

<https://github.com/Z3Prover/z3/issues/3973>

# Bug Findings

Status	Z3	CVC4	Total
Reported	811	281	1,092
Confirmed	578	241	819
Fixed	521	164	106
Duplicate	85	18	79

Bug status as of 30 Oct 2020

Z3 Soundness Bug #2832

```
$ cat bug.smt2
(declare-const a (_ BitVec 8))
(declare-const b (_ BitVec 8))
(declare-const c (_ BitVec 8))
(assert (= (bvxnor a b c)
            (bvxnor (bvxnor a b) c)))
(check-sat)
```

CVC4 Soundness Bug #3497

```
$ cat bug.smt2
(declare-fun x () String)
(declare-fun y () String)
(assert (= (str.indexof x y 1) < (str.len x)))
(assert (str.contains x y))
(check-sat)

$ z3 bug.smt2
sat ✓

$ cvc4 bug.smt2
unsat ✗
```

**Root Cause: Missed boundary condition**

CVC4 Soundness Bug #4469

Z3 Soundness Bug #2830

```
$ cat bug.smt2
(declare-fun a () Int)
(declare-fun b (Int) Bool)
(assert (b 0))
(push)
(assert (distinct true (= a 0) (not (b 0))))
(check-sat)

$ cvc4 bug.smt2
unsat ✓

$ z3 bug.smt2
sat ✗
```

```
$ cat bug.smt2
(set-logic QF_AUFBVЛИA)
(declare-fun a () Int)
(declare-fun b (Int) Int)
(assert (distinct (b a)
                  (b (b a))))
(check-sat)

Labels
          bug   major
```

```
$ z3 bug.smt2
sat ✓

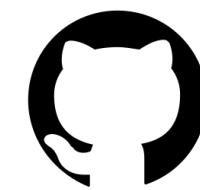
$ cvc4 bug.smt2
unsat ✗
```

# Yin-Yang Umbrella Release

OpFuzz

+

Semantic Fusion [PLDI '20]



[github.com/testsmt](https://github.com/testsmt)